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# Optimal test case generation using game theory

Making tests robustly exploit and explore

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Léo Henry

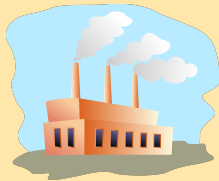
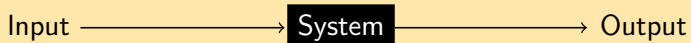
supervisors:

Nicolas Markey    Thierry Jéron

Univ. Rennes, INRIA & CNRS

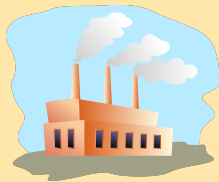
Rennes (France)

# Black-box conformance timed testing



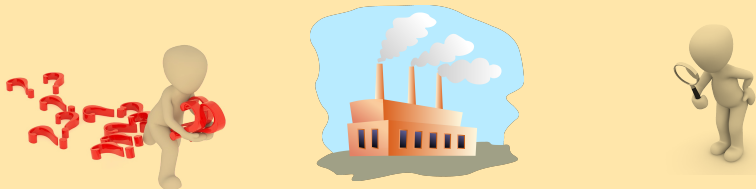
# Black-box conformance timed testing

Input → System → Output



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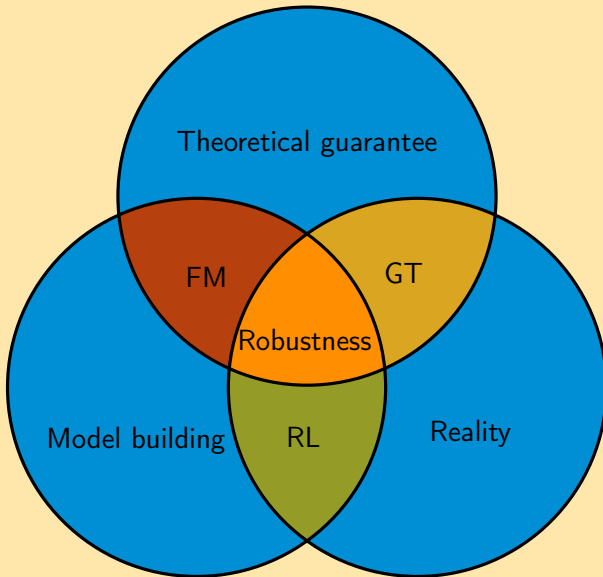


Conformance testing

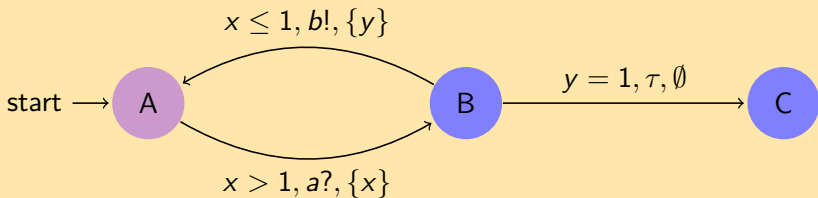
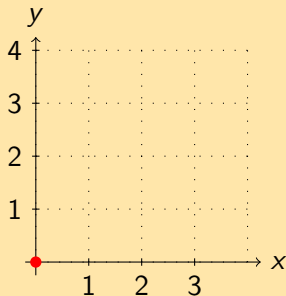
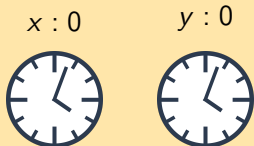


Timed testing

## At the edge of many domains



# A model for timed systems: TAIO

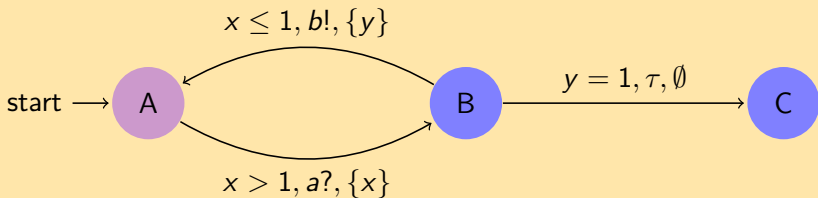
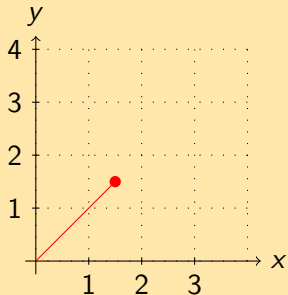


# A model for timed systems: TAIO

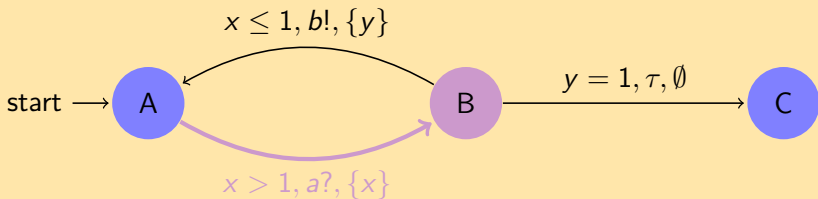
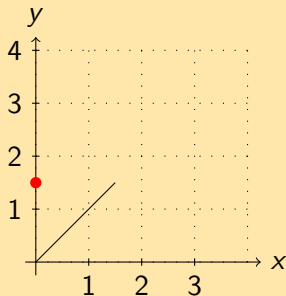
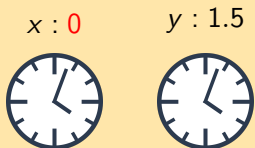
$x : 1.5$



$y : 1.5$

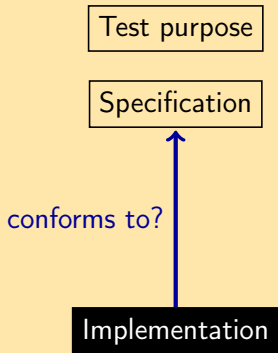


# A model for timed systems: TAIO



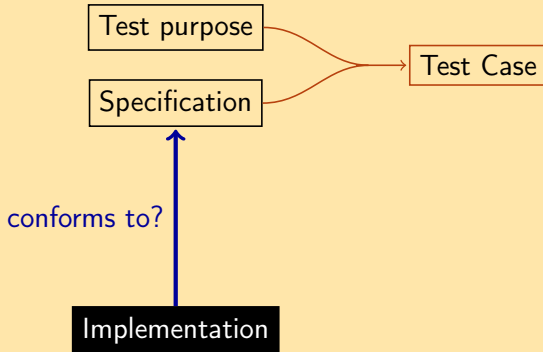


# Setup



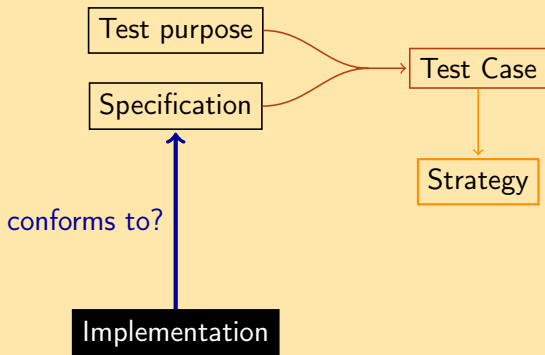
# Setup

## Formal Methods



# Setup

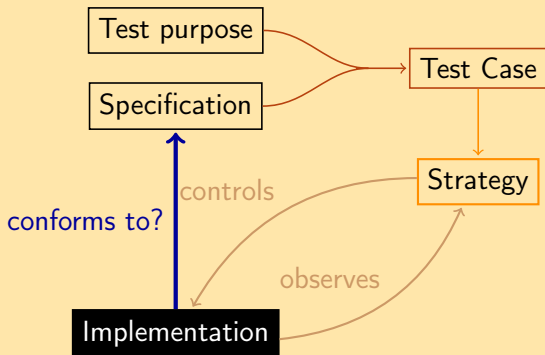
## Formal Methods



## Game Theory

# Setup

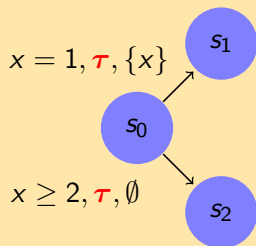
## Formal Methods



## Game Theory

# First challenges

Partial observability<sup>1</sup> Consequence of the black-box assumption.

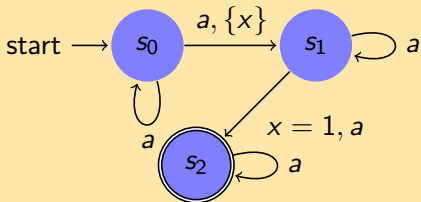
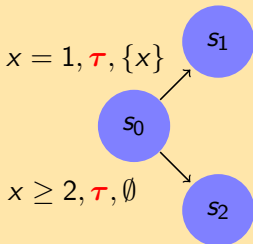


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<sup>1</sup>Bertrand, Jérôme, Stainer, and Krichen, "Off-line test selection with test purposes for non-deterministic timed automata", 2012, *Logical Methods in Computer Science*.

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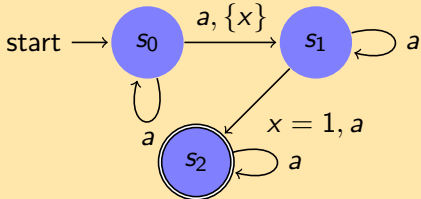
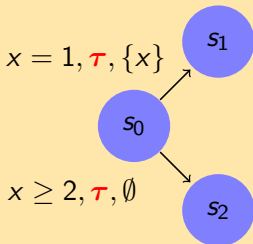


No determinizability<sup>1</sup> A deterministic equivalent does not always exist.

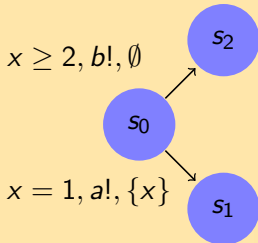
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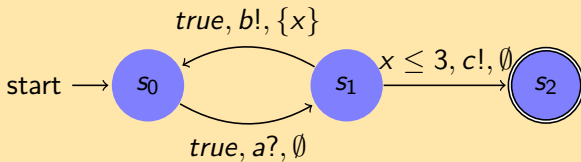
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Partial controllability Price of design liberty.

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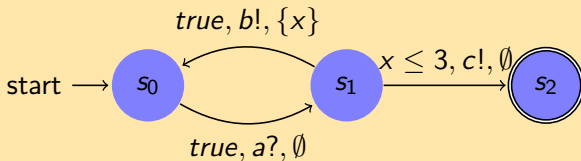
## Difficult timed games



<sup>2</sup>Henry, Jéron, and Markey, "Control Strategies for Off-Line Testing of Timed Systems", 2018, *SPIN*.



## Difficult timed games

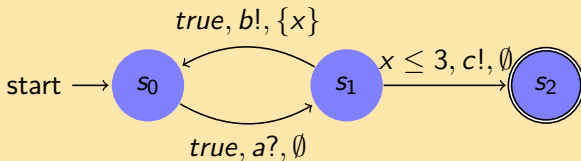


We rely on the *fairness* of the implementation.

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## Difficult timed games

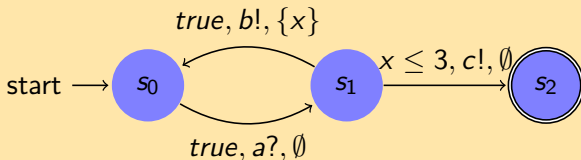


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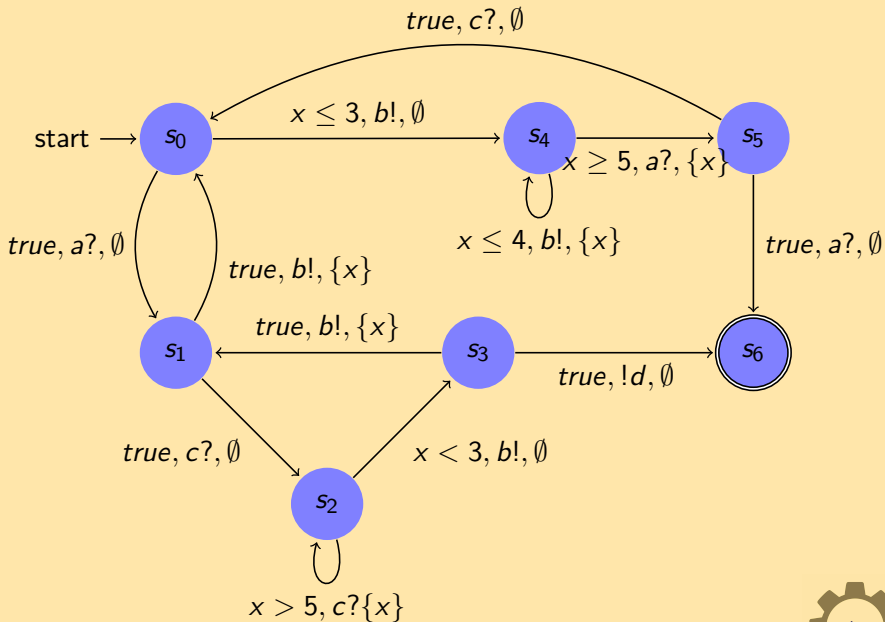


We rely on the *fairness* of the implementation. We can construct a strategy that is *winning*, and create test cases that are,  $\forall \mathcal{I} \in \mathcal{I}(\mathcal{S}), \forall (\mathcal{G}, f) \in \mathcal{TC}(\mathcal{S})$ :

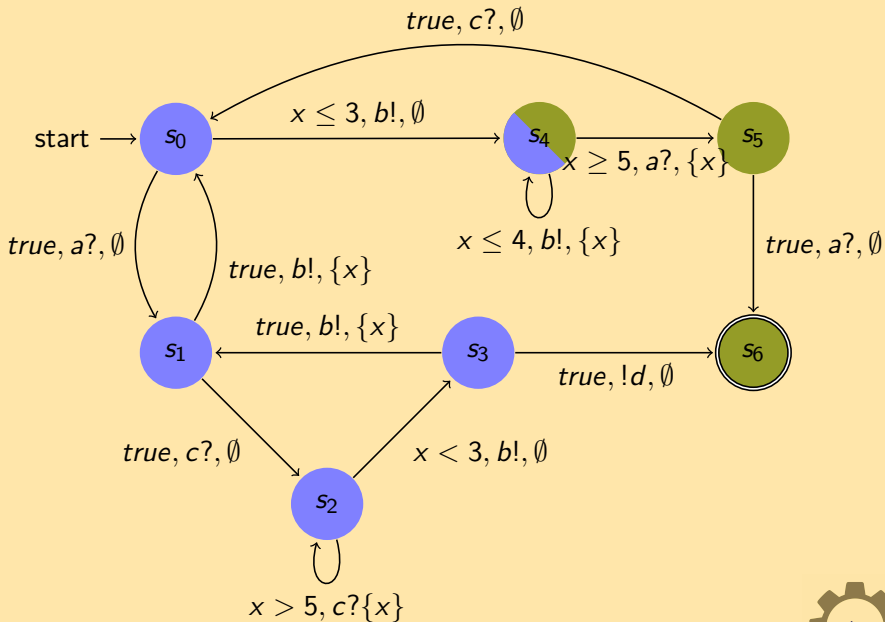
- ▶ sound:  $\mathcal{I} \text{ fails } (\mathcal{G}, f) \Rightarrow \neg(\mathcal{I} \text{ tioco } \mathcal{S})$ ;
- ▶ Up to the determinization approximations:
  - ▶ strict:  $\neg(\text{Behaviour}(\mathcal{G}, f, \mathcal{I}) \text{ tioco } \mathcal{S}) \Rightarrow \mathcal{I} \text{ fails } (\mathcal{G}, f)$ ;
  - ▶ exhaustive:  $\neg(\mathcal{I} \text{ tioco } \mathcal{S}) \Rightarrow \exists (\mathcal{G}, f) \in \mathcal{TC}(\mathcal{S}), \mathcal{I} \text{ fails } (\mathcal{G}, f)$ ;
  - ▶ precise: there is no approximation in the acceptance condition.

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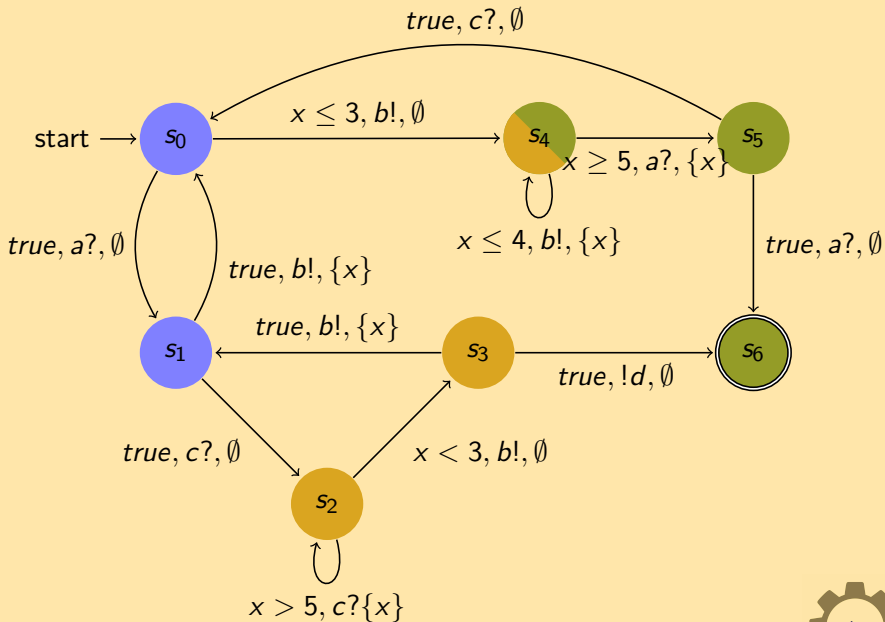
# A motivating example



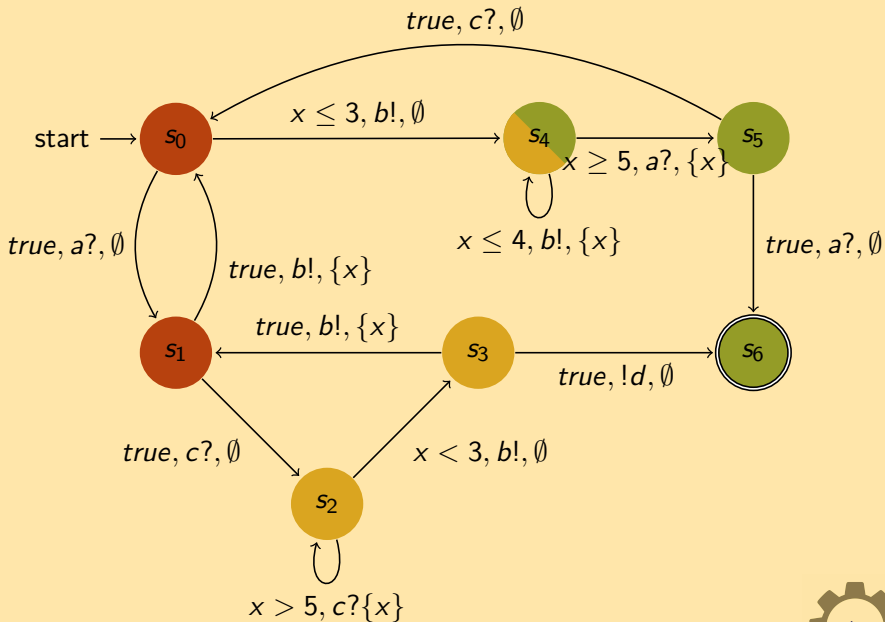
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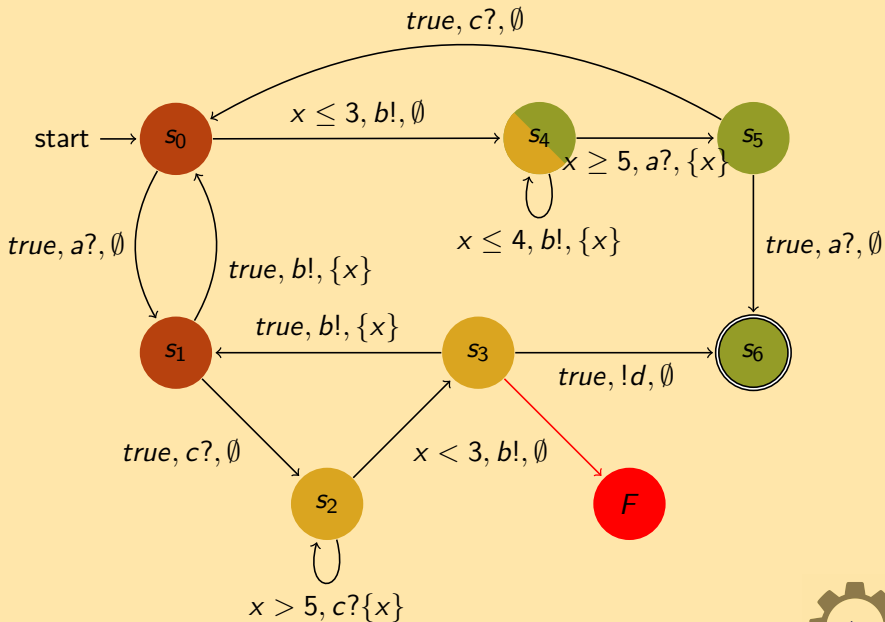
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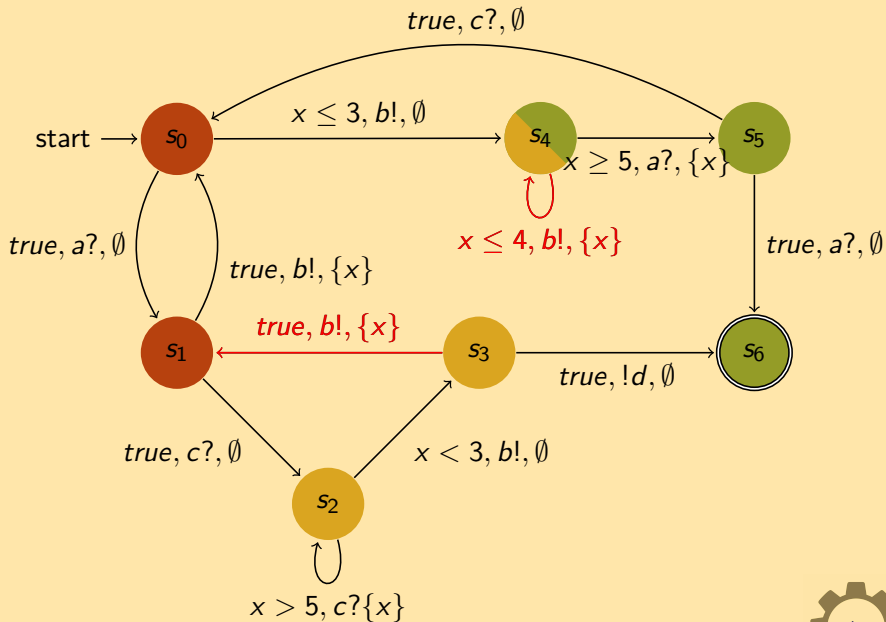


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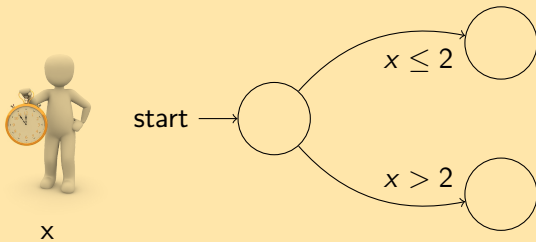
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# Model weaknesses

## Reality strikes back

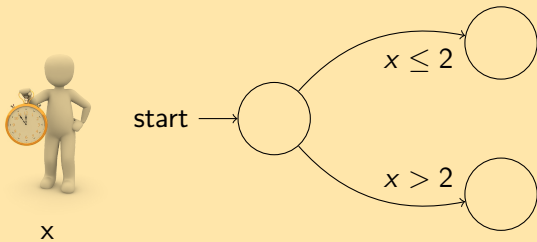
Robustness What precision do we require in the measure of time?



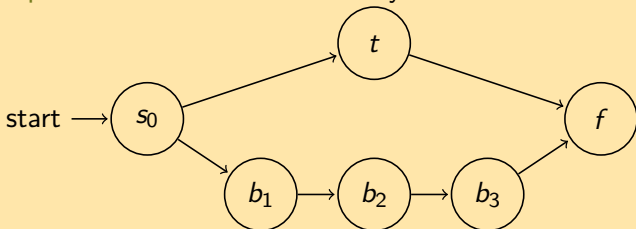
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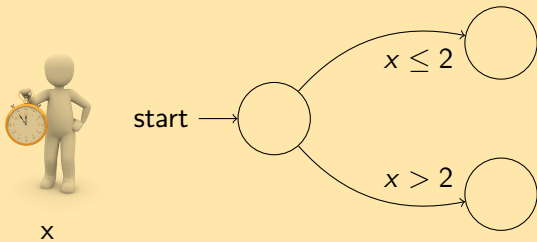
**Implementation freedom** We only want to enforce " $\mathcal{I}$  conforms  $\mathcal{S}$ "



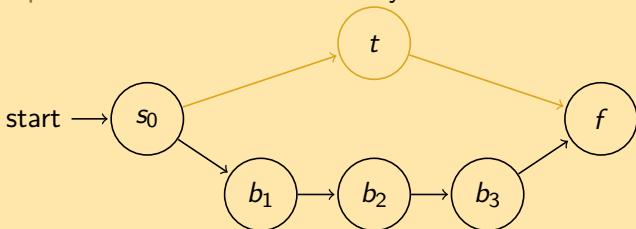
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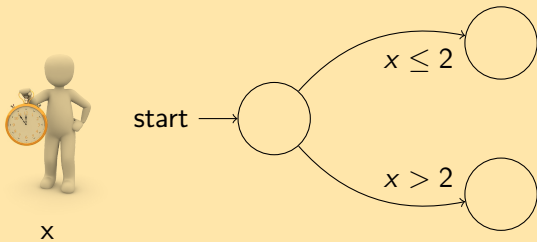
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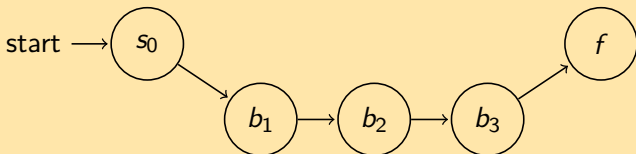
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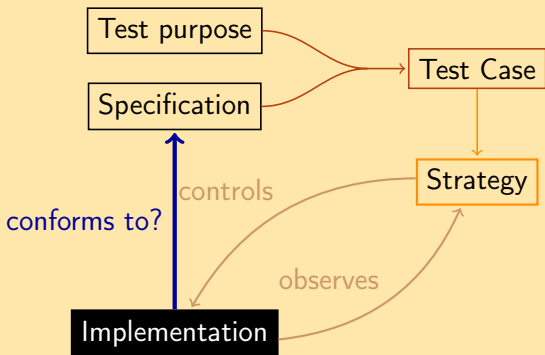
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# Reinforcement learning

Learning from the implementation

## Formal Methods

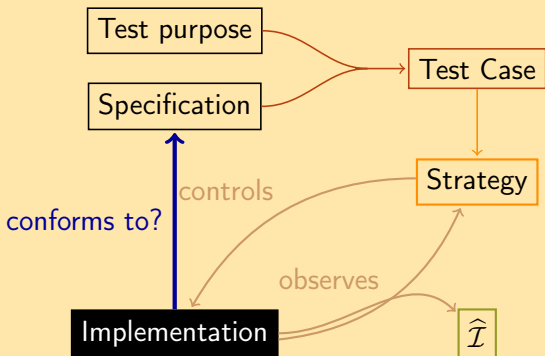


Game Theory

# Reinforcement learning

Learning from the implementation

## Formal Methods

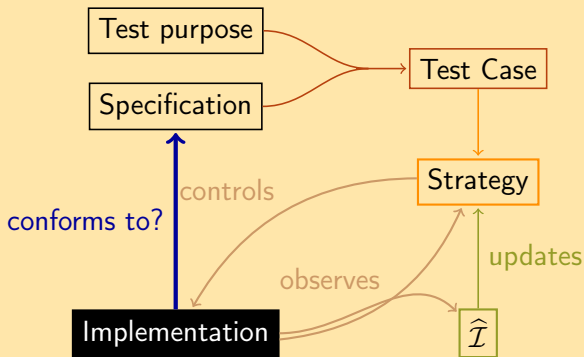


Game Theory

# Reinforcement learning

Learning from the implementation

## Formal Methods



Game Theory

Reinforcement Learning



# Current and ongoing work

What did I do all this time?

What is done:



A paper on difficult games for tests... and a journal version;



A bibliographic study on learning and reinforcement learning;

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# Current and ongoing work

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A bibliographic study on learning and reinforcement learning;

What is ongoing:



A journal version of [BJM18] on determinization of TAs for diagnosis;



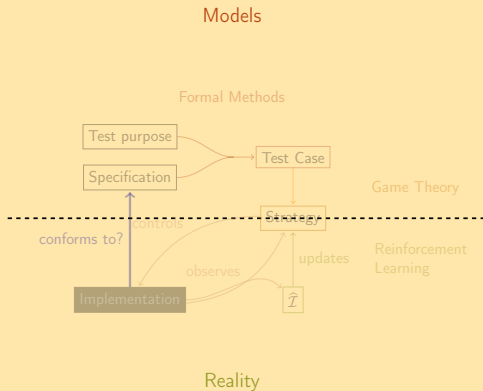
The generalization to games with inconclusive states.

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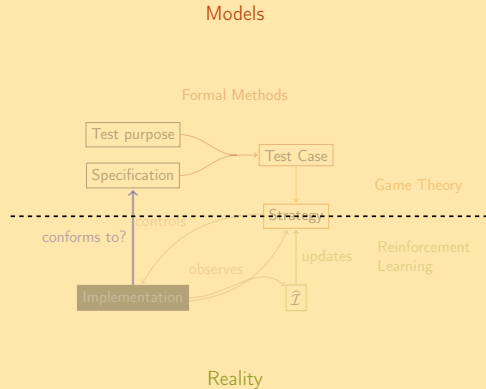
# To conclude

- Formal test generation is at the edge between reality and models.



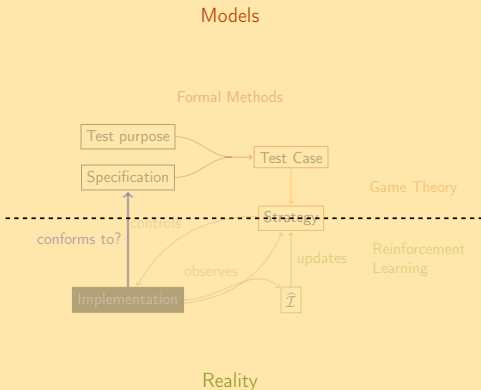
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- ▶ Formal test generation is at the edge between reality and models.
- ▶ Information from both the model and the real world *should* be exploited.



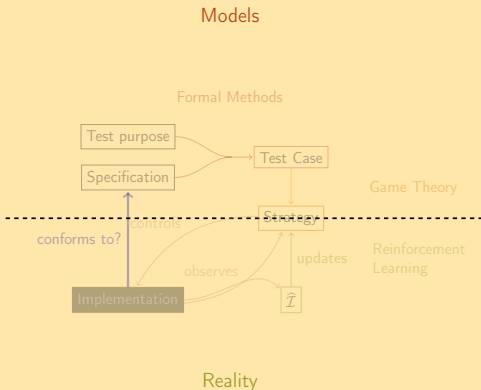
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Game Theory

Formal Methods

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